

$$a) \int (-3x^3 + \frac{1}{12}x^2 + 8x) dx = -\frac{3}{4}x^4 + \frac{1}{36}x^3 + 4x^2 + C$$

$$b) \int (e^x - e^{-x}) dx = e^x + e^{-x} + C$$

$$c) \int (\sin x + x^2) dx = -\cos x + \frac{x^3}{3} + C$$

$$d) \int \left( \frac{1}{x} + \frac{1}{x^2} \right) dx = \ln|x| - \frac{1}{x}$$

$$e) \int (\sqrt{x} + \frac{1}{4}\sqrt[6]{x}) dx = \int (x^{\frac{1}{2}} + \frac{1}{4}x^{\frac{1}{6}}) dx =$$

$$= \frac{2}{3}x^{\frac{3}{2}} + \frac{1}{4} \cdot \frac{6}{7}x^{\frac{1+6}{6}} + C =$$

$$= \frac{2}{3}x^{\frac{3}{2}} + \frac{3}{14}x^{\frac{7}{6}} + C$$

$$= \frac{2}{3} \cdot \sqrt{x^3} + \frac{3}{14} \cdot \sqrt[6]{x^7}$$

⚠️

$$\int (\sin x + x^2) dt = \underbrace{(\sin x + x^2)}_{\substack{\text{Formvariable} \\ \text{Konstante}}} \cdot t + C$$

$$\int (\sin 2t + x^2) dt =$$

$$= -\frac{1}{2} \cos 2t + x^2 \cdot t + C$$

$$\int e^{4x} dx = \frac{1}{4} e^{4x} + C$$

$$\int 2^x dx = \int (e^{\ln 2})^x dx =$$

$$\boxed{a = e^{\ln a}}$$

$$\int e^{\ln 2 \cdot x} dx = \frac{1}{\ln 2} e^{\ln 2 \cdot x} = \frac{1}{\ln 2} \cdot 2^x$$

$$f(x) = \frac{3}{x-5}$$

DL,  $x \rightarrow \pm\infty$   $x=5$

$$\lim_{h \rightarrow 0} f(5 \pm h) = \lim_{h \rightarrow 0} \frac{3}{5 \pm h - 5} = \lim_{h \rightarrow 0} \frac{3}{\pm h} = \pm\infty$$

$$f(x) = \frac{2e^x}{e^x + 9}$$

$$f'(x) = \frac{(e^x + 9)2e^x - 2e^x \cdot e^x}{(e^x + 9)^2} =$$
$$= \frac{18e^x}{(e^x + 9)^2}$$

$$e^x \cdot e^x$$
$$e^{2x} \neq e^{(x^2)}$$